



**Class XII - Math**  
**Chapter: Differential Calculus**  
**Concepts and Formulae**

S.No	Chapter	Formula	
1	<b>Continuity &amp; Differentiability</b>	<b>1.1</b>	<b>Continuity of a function</b> <ul style="list-style-type: none"> <li>A function <math>f(x)</math> is said to be continuous at a point <math>c</math> if,  <math display="block">\lim_{x \rightarrow c^-} f(x) = \lim_{x \rightarrow c^+} f(x) = f(c)</math> </li> </ul>
		<b>1.2</b>	<b>Algebra of Continuous Functions</b> If $f$ and $g$ are continuous functions, then <ul style="list-style-type: none"> <li><math>(f \pm g)(x) = f(x) \pm g(x)</math> is continuous</li> <li><math>(f.g)(x) = f(x).g(x)</math> is continuous</li> <li><math>\left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)}</math> (where <math>g(x) \neq 0</math>) is continuous</li> </ul>
		<b>1.3</b>	<b>Differentiability of a function</b> <ul style="list-style-type: none"> <li>A function <math>f</math> is differentiable at a point <math>c</math>                      If, LHD=RHD                      i.e <math display="block">\lim_{h \rightarrow 0^-} \frac{f(c+h) - f(c)}{h} = \lim_{h \rightarrow 0^+} \frac{f(c+h) - f(c)}{h}</math> </li> <li>Derivative of a function <math>f</math> is <math>f'(x)</math> which is  <math display="block">f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}</math> </li> <li>Every differentiable function is continuous, but converse is not true.</li> </ul>
		<b>1.3</b>	<b>Algebra of Derivatives</b> If $u$ & $v$ are two functions which are differentiable, then <ul style="list-style-type: none"> <li><math>(u \pm v)' = u' \pm v'</math></li> <li><math>(uv)' = u'v + uv'</math> (Product rule)</li> <li><math>\left(\frac{u}{v}\right)' = \frac{u'v - uv'}{v^2}</math> (Quotient rule)</li> </ul>
		<b>1.4</b>	<b>Derivatives of Functions</b> <ul style="list-style-type: none"> <li><math display="block">\frac{d}{dx} x^n = nx^{n-1}</math> </li> </ul>



# IMPORTANT FORMULAE

		<ul style="list-style-type: none"> <li>▪ <math>\frac{d}{dx}(\sin x) = \cos x</math></li> <li>▪ <math>\frac{d}{dx}(\cos x) = -\sin x</math></li> <li>▪ <math>\frac{d}{dx}(\tan x) = \sec^2 x</math></li> <li>▪ <math>\frac{d}{dx}(\cot x) = -\operatorname{cosec}^2 x</math></li> <li>▪ <math>\frac{d}{dx}(\sec x) = \sec x \tan x</math></li> <li>▪ <math>\frac{d}{dx}(\operatorname{cosec} x) = -\operatorname{cosec} x \cot x</math></li> <li>▪ <math>\frac{d}{dx}(\sin^{-1} x) = \frac{1}{\sqrt{1-x^2}}</math></li> <li>▪ <math>\frac{d}{dx}(\cos^{-1} x) = -\frac{1}{\sqrt{1-x^2}}</math></li> <li>▪ <math>\frac{d}{dx}(\tan^{-1} x) = \frac{1}{1+x^2}</math></li> <li>▪ <math>\frac{d}{dx}(\cot^{-1} x) = -\frac{1}{1+x^2}</math></li> <li>▪ <math>\frac{d}{dx}(\sec^{-1} x) = \frac{1}{x\sqrt{x^2-1}}</math></li> <li>▪ <math>\frac{d}{dx}(\operatorname{cosec}^{-1} x) = \frac{-1}{x\sqrt{x^2-1}}</math></li> <li>▪ <math>\frac{d}{dx}(e^x) = e^x</math></li> <li>▪ <math>\frac{d}{dx}(\log x) = \frac{1}{x}</math></li> </ul>
		<p><b>1.5 Chain Rule</b></p> <p>If <math>f = v \circ u</math>, <math>t = u(x)</math> &amp; if both <math>\frac{dt}{dx}</math> and <math>\frac{dv}{dt}</math>, exists then,</p> $\frac{df}{dx} = \frac{dv}{dt} \cdot \frac{dt}{dx}$
		<p><b>1.6 Implicit Functions</b></p> <p>If it is not possible to "separate" the variables <math>x</math> &amp; <math>y</math> then function <math>f</math> is known as implicit function.</p>



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		<p><b>1.7 Logarithms</b>  <math>\log(xy) = \log x + \log y</math>  <math>\log\left(\frac{x}{y}\right) = \log x - \log y</math>  <math>\log(x^y) = y \log x</math>  <math>\log_a x = \frac{\log_b x}{\log_b a}</math></p>
		<p><b>1.8 Logarithmic Differentiation</b>          Differentiation of <math>y = a^x</math>          Taking logarithm on both sides  <math>\log y = \log a^x</math>          Using property of logarithms  <math>\log y = x \log a</math>          Now differentiating the implicit function  <math>\frac{1}{y} \cdot \frac{dy}{dx} = \log a</math>  <math>\frac{dy}{dx} = y \log a = a^x \log a</math></p>
		<p><b>1.9 Parametric Differentiation</b>          Functions of the form <math>x = f(t)</math> and <math>y = g(t)</math> are parametric functions.</p> $\frac{dy}{dx} = \frac{\frac{dy}{dt}}{\frac{dx}{dt}}$ $\frac{dy}{dx} = \frac{dy}{dt} \times \frac{dt}{dx}$
		<p><b>1.1 Mean Value Theorems</b></p> <ul style="list-style-type: none"> <li>▪ <b>Rolle's Theorem:</b> If <math>f : [a, b] \rightarrow \mathbf{R}</math> is continuous on <math>[a, b]</math> and differentiable on <math>(a, b)</math> such that <math>f(a) = f(b)</math>, then there exists some <math>c</math> in <math>(a, b)</math> such that <math>f'(c) = 0</math></li> <li>▪ <b>Mean Value Theorem:</b> If <math>f : [a, b] \rightarrow \mathbf{R}</math> is continuous on <math>[a, b]</math> &amp; differentiable on <math>(a, b)</math>. Then there exists some <math>c</math> in <math>(a, b)</math> such that <math>f'(c) = \lim_{h \rightarrow 0} \frac{f(b) - f(a)}{b - a}</math></li> </ul>



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2	Application of derivatives	2.1	<p><b>Increasing &amp; Decreasing functions</b>            Let <math>I</math> be an open interval contained in domain of a real valued function <math>f</math>. Then <math>f</math> is said to be:</p> <ul style="list-style-type: none"> <li>▪ Increasing on <math>I</math> if <math>x_1 &lt; x_2</math> in <math>I</math>  <math>\Rightarrow f(x_1) \leq f(x_2)</math> for all <math>x_1, x_2 \in I</math></li> <li>▪ Strictly increasing on <math>I</math> if <math>x_1 &lt; x_2</math> in <math>I</math>  <math>\Rightarrow f(x_1) &lt; f(x_2)</math> for all <math>x_1, x_2 \in I</math></li> <li>▪ Decreasing on <math>I</math> if <math>x_1 &lt; x_2</math> in <math>I</math>  <math>\Rightarrow f(x_1) \geq f(x_2)</math> for all <math>x_1, x_2 \in I</math></li> <li>▪ Strictly decreasing on <math>I</math> if <math>x_1 &lt; x_2</math> in <math>I</math>  <math>\Rightarrow f(x_1) &gt; f(x_2)</math> for all <math>x_1, x_2 \in I</math></li> </ul> <p><b>Theorem:</b>            Let <math>f</math> be a continuous function on <math>[a, b]</math> and differentiable on <math>(a, b)</math>. Then            (a) <math>f</math> is increasing in <math>[a, b]</math> if <math>f'(x) &gt; 0</math> for each <math>x \in (a, b)</math>            (b) <math>f</math> is decreasing in <math>[a, b]</math> if <math>f'(x) &lt; 0</math> for each <math>x \in (a, b)</math>            (c) <math>f</math> is constant in <math>[a, b]</math> if <math>f'(x) = 0</math> for each <math>x \in (a, b)</math></p>
		2.3	<p><b>Tangents &amp; Normals</b></p> <ul style="list-style-type: none"> <li>▪ The equation of the tangent at <math>(x_0, y_0)</math> to the curve <math>y = f(x)</math> is:  <math>y - y_0 = f'(x_0)(x - x_0)</math></li> <li>▪ Slope of a tangent = <math>\frac{dy}{dx} = \tan \theta</math></li> <li>▪ The equation of the normal to the curve <math>y = f(x)</math> at <math>(x_0, y_0)</math> is:  <math>(y - y_0)f'(x_0) + (x - x_0) = 0</math></li> <li>▪ Slope of Normal = <math>\frac{-1}{\text{slope of the tangent}}</math></li> </ul>
		2.4	<p><b>First Derivative Test</b>            Let <math>f</math> be a function defined on an open interval <math>I</math>. Let <math>f</math> be continuous at a critical point <math>c</math> in <math>I</math>. Then</p> <ul style="list-style-type: none"> <li>▪ If <math>f'(x) &gt; 0</math> at every point sufficiently</li> </ul>



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			<p>close to and to the left of <math>c</math> &amp; <math>f'(x) &lt; 0</math> at every point sufficiently close to and to the right of <math>c</math>, then <math>c</math> is a point of local maxima.</p> <ul style="list-style-type: none"> <li>If <math>f'(x) &lt; 0</math> at every point sufficiently close to and to the left of <math>c</math>, <math>f'(x) &gt; 0</math> at every point sufficiently close to and to the right of <math>c</math>, then <math>c</math> is a point of local minima.</li> <li>If <math>f'(x)</math> does not change sign as <math>x</math> increases through <math>c</math>, then point <math>c</math> is called point of inflexion</li> </ul>
		<b>2.5</b>	<p><b>Second Derivative test</b></p> <p>Let <math>f</math> be a function defined on an interval <math>I</math> &amp; <math>c \in I</math>. Let <math>f</math> be twice differentiable at <math>c</math>. Then</p> <ul style="list-style-type: none"> <li><math>x = c</math> is a point of local maxima if <math>f'(c) = 0</math> &amp; <math>f''(c) &lt; 0</math>.</li> <li><math>x = c</math> is a point of local minima if <math>f'(c) = 0</math> and <math>f''(c) &gt; 0</math></li> <li>The test fails if <math>f'(c) = 0</math> &amp; <math>f''(c) = 0</math>. By first derivative test, find whether <math>c</math> is a point of maxima, minima or a point of inflexion.</li> </ul>
		<b>2.6</b>	<p><b>Differential Approximations</b></p> <ul style="list-style-type: none"> <li>Let <math>y = f(x)</math>, <math>\Delta x</math> be small increments in <math>x</math> and <math>\Delta y</math> be small increments in <math>y</math> corresponding to the increment in <math>x</math>, i.e., <math>\Delta y = f(x + \Delta x) - f(x)</math>. Then</li> </ul> $\Delta y = \left(\frac{dy}{dx}\right) \Delta x \text{ or } dy = \left(\frac{dy}{dx}\right) \Delta x$ $\Delta y \approx dy \text{ and } \Delta x \approx dx$