



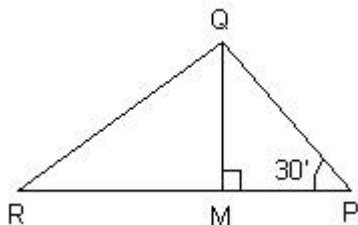
**Mathematics**  
**Class X**  
**TOPPER SAMPLE PAPER-1**  
**SOLUTIONS**

Ans1 HCF x LCM = Product of the 2 numbers  
 126 x LCM = 252 x 378  
 LCM = 756 (1 Mark)

Ans2 The zeroes are -1, 4  
 $\therefore p(x) = (x+1)(x-4) = x^2 - 3x - 4$  (1 Mark)

Ans3 For intersecting lines:  
 $\frac{a_1}{a_2} \neq \frac{b_1}{b_2} \Rightarrow \frac{13}{k} \neq \frac{23}{-46}$   
 $\Rightarrow k \neq -26$  (1 Mark)

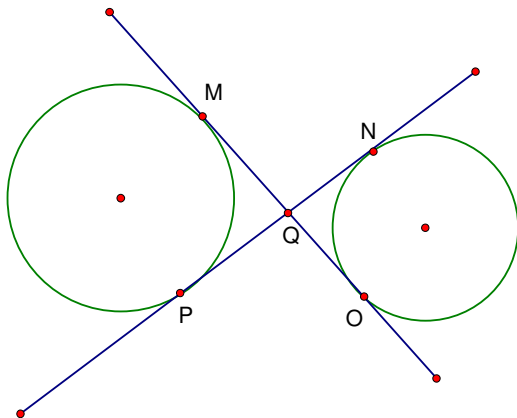
Ans4



Since  $PR^2 - PQ^2 = QR^2$   
 $\Rightarrow PR^2 = QR^2 + PQ^2$   
 $\Rightarrow \angle RQP = 90^\circ$  (Converse of Pythagoras Theorem)  
 Therefore, In  $\Delta PQM$   
 Since  $\angle QPM = 30^\circ$  and  $\angle QMP = 90^\circ$   
 So  $\angle MQP = 60^\circ$   
 Hence,  $\angle MQR = 30^\circ$  (1 Mark)



Ans5



$$\begin{aligned}
 OM &= MQ + QO \\
 &= QP + QN \quad [\text{Since Tangents from external point are equal}] \\
 &= PN = 9\text{cm} \quad (1 \text{ Mark})
 \end{aligned}$$

Ans6 The two curves namely less than and more than ogives intersect at the median so the point of intersection is (45.5, 75)  
(1 Mark)

Ans7 Total outcomes = HH, TT, HT, TH

Favourable outcomes = HH

$$P(E : \text{Both Heads}) = \frac{1}{4} \quad (1 \text{ Mark})$$

Ans8 Let  $a_3$  and  $a_4$  be the third and fourth term of the AP  
According to given Condition

$$\begin{aligned}
 3.a_3 &= 4.a_4 \\
 \Rightarrow 3(a + 2d) &= 4(a + 3d) \\
 \Rightarrow a &= -6d \\
 \Rightarrow a + 6d &= 0 \\
 \Rightarrow a_7 &= 0
 \end{aligned} \quad (1 \text{ Mark})$$



Ans9  $\sin \alpha + \cos \alpha = \sqrt{2} \sin \alpha$

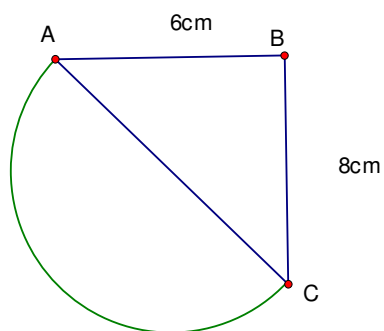
$$\cos \alpha = \sin \alpha (\sqrt{2} - 1)$$

$$\frac{\cos \alpha}{\sin \alpha} = \sqrt{2} - 1$$

$$\cot \alpha = \sqrt{2} - 1$$

(1 Mark)

Ans10



$$\begin{aligned} AC &= \sqrt{AB^2 + BC^2} && \text{(Using Pythagoras Theorem)} \\ &= \sqrt{6^2 + 8^2} \\ &= \sqrt{36 + 64} \\ &= 10 \text{ cm} \end{aligned}$$

$$\begin{aligned} \text{Circumference of semi circle} &= \pi r \\ &= 3.14 \times 5 \\ &= 15.70 \text{ cm} \end{aligned}$$

$$\begin{aligned} \therefore \text{Perimeter} &= 6 + 8 + 15.7 \\ &= 29.7 \text{ cm} \end{aligned}$$

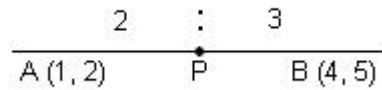
(1 Mark)



**SECTION B**

Ans11 Since,  $AP = \frac{2}{5} AB$

So  $AP: PB = 2: 3$



P divides AB in 2:3 ratios

(1 mark)

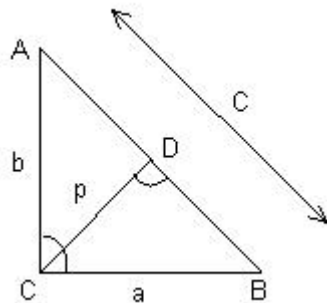
$$P\left(\frac{2 \times 4 + 3 \times 1}{5}, \frac{2 \times 5 + 3 \times 2}{5}\right)$$

$\left(\frac{1}{2}\right)$  mark

$$P\left(\frac{11}{5}, \frac{16}{5}\right)$$

$\left(\frac{1}{2}\right)$  mark

Ans12



$$\begin{aligned} \text{Area } (\Delta ACB) &= \frac{1}{2} AC \cdot CB \\ &= \frac{1}{2} a \cdot b \end{aligned}$$

$$\text{Also, area } (\Delta ACB) = \frac{1}{2} \cdot AB \cdot CD$$

$\left(\frac{1}{2}\right)$  mark

$$= \frac{1}{2} cp$$



$$\Rightarrow \frac{1}{2} ab = \frac{1}{2} cp \quad \left(\frac{1}{2} \text{ mark}\right)$$

$$\Rightarrow ab = cp$$

Now  $\frac{1}{a^2} + \frac{1}{b^2} = \frac{b^2 + a^2}{a^2 b^2}$

$$= \frac{c^2}{a^2 b^2} \quad (\text{By Pythagoras theorem})$$

$$= \frac{c^2}{a^2 b^2}$$

$$= \frac{c^2}{c^2 p^2} \quad (\text{Since, } ab = cp)$$

$$= \frac{1}{p^2}$$

Hence Proved (1 Mark)

Ans13  $3(2x + y) = 7xy \Rightarrow 6x + 3y = 7xy \quad (1)$

$3(x + 3y) = 11xy \Rightarrow 3x + 9y = 11xy \quad (2)$

Eq (2)  $\times 2$  gives:  $6x + 18y = 22xy \quad (3)$

When  $x \neq 0$  and  $y \neq 0$  eq(1) - eq(3) gives

$-15y = -15xy \quad \left(\frac{1}{2} \text{ mark}\right)$

$\Rightarrow x = 1 \quad \left(\frac{1}{2} \text{ mark}\right)$

$\Rightarrow y = \frac{3}{2} \quad \left(\frac{1}{2} \text{ mark}\right)$

Also  $x = 0, y = 0$  is a solution. (1/2 mark)



Ans14 August has 31 days  
 $\Rightarrow$  4 weeks and 3 days.

So 4 weeks means 4 Wednesdays

Now remaining 3 days can be

S M T	T W Th	Th F Sa	Sa. S M	
M T W	W Th F	F Sa S		(1 Mark)

Favorable outcomes are = M T W

T W Th  $\left(\frac{1}{2}\right)$  mark

W Th F

$\therefore P(3 \text{ Wednesdays}) = \frac{3}{7}$   $\left(\frac{1}{2}\right)$  mark

Ans15  $\sin(A + B) = 1$

Since  $\sin 90^\circ = 1$

$A + B = 90^\circ$  (1)  $\left(\frac{1}{2}\right)$  mark

$$\cos(A - B) = \frac{\sqrt{3}}{2}$$

since  $\cos 30^\circ = \frac{\sqrt{3}}{2}$

$A - B = 30^\circ$  (2)  $\left(\frac{1}{2}\right)$  mark

Solving (1) and (2)

$A = 60^\circ$   $\left(\frac{1}{2}\right)$  mark

$B = 30^\circ$   $\left(\frac{1}{2}\right)$  mark

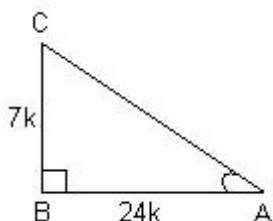
OR



$$\tan A = \frac{7}{24}$$

So the ratio of adjacent and opposite side of the triangle is in the ratio 7:24

Let the common ratio term be k



Using Pythagoras Theorem

$$AC = 25 k. \quad \left(\frac{1}{2} \text{ mark}\right)$$

Consider  $\sqrt{\frac{1 - \cos A}{1 + \cos A}}$

$$= \sqrt{\frac{1 - \frac{24}{25}}{1 + \frac{24}{25}}} \quad (1 \text{ Mark})$$

$$= \sqrt{\frac{1}{49}} = \frac{1}{7} \quad \left(\frac{1}{2} \text{ mark}\right)$$

**SECTION C**

Ans16 Let us assume  $\sqrt{5}$  is rational.

$$\Rightarrow \sqrt{5} = \frac{p}{q} \text{ Where } p \text{ and } q \text{ are co prime integers and } q \neq 0$$

$$\left(\frac{1}{2} \text{ mark}\right)$$

$$\Rightarrow \sqrt{5}q = p$$

$$\Rightarrow 5q^2 = p^2$$

$$\Rightarrow 5 \text{ divides } p^2$$

$$\Rightarrow 5 \text{ divides } p \quad (1)$$

$$\left(\frac{1}{2} \text{ mark}\right)$$



So  $p = 5a$  for some integer  $a$

$\left(\frac{1}{2} \text{ mark}\right)$

Substituting  $p = 5a$  in  $5q^2 = p^2$

$$5q^2 = 25a^2$$

$$\Rightarrow q^2 = 5a^2$$

$$\Rightarrow 5 \text{ divides } q^2$$

$$\Rightarrow 5 \text{ divides } q \quad (2)$$

$\left(\frac{1}{2} \text{ mark}\right)$

From (1) & (2) 5 is a common factor to  $p$  and  $q$  which contradicts the fact that  $P$  and  $q$  are co prime

$\therefore$  Our assumption is wrong and hence  $\sqrt{5}$  is irrational.  $\left(\frac{1}{2} \text{ mark}\right)$

Ans17 Let  $A(x, y)$  be the required point which is at a distance of 5 units from the point  $P(0,5)$  and 3 units from  $Q(0,1)$

So  $AP = 5$  and  $AQ = 3$

$$\Rightarrow \sqrt{(x-0)^2 + (y-5)^2} = 5$$

$\left(\frac{1}{2} \text{ mark}\right)$

$$\Rightarrow (x-0)^2 + (y-5)^2 = 25$$

$$\Rightarrow x^2 + y^2 - 10y = 0 \quad (1)$$

$\left(\frac{1}{2} \text{ mark}\right)$

$$\sqrt{(x-0)^2 + (y-1)^2} = 3$$

$\left(\frac{1}{2} \text{ mark}\right)$

$$x^2 + (y-1)^2 = 9$$

$$x^2 + y^2 - 2y - 8 = 0 \quad (2)$$

$\left(\frac{1}{2} \text{ mark}\right)$

Equation (1) - Equation (2) gives:

$$-8y + 8 = 0 \Rightarrow y = 1$$





Substituting  $y = 1$  in (1)

$$x^2 - 9 = 0 \Rightarrow x = \pm 3$$

$\therefore$  The required points are (3, 1) and (-3, 1) ( $\frac{1}{2}$  mark)

Ans18  $(\sin A + \operatorname{cosec} A)^2 + (\cos A + \sec A)^2$

$$= \sin^2 A + \operatorname{cosec}^2 A + 2 \sin A \operatorname{cosec} A + \cos^2 A + \sec^2 A + 2 \cos A \sec A$$

( $\frac{1}{2}$  mark)

$$= (\sin^2 A + \cos^2 A) + 2 + 2 + \operatorname{cosec}^2 A + \sec^2 A$$

(Since  $\sin A \cdot \operatorname{cosec} A = 1$  and  $\cos A \cdot \sec A = 1$ ) (1Mark)

$$= 1 + 2 + 2 + 1 + \cot^2 A + 1 + \tan^2 A$$

(Since,  $\operatorname{cosec}^2 A = 1 + \cot^2 A$  and  $\sec^2 A = 1 + \tan^2 A$ ) (1 Mark)

$$= 7 + \cot^2 A + \tan^2 A$$

=RHS ( $\frac{1}{2}$  mark)

OR

$$(1 + \cot \theta - \operatorname{cosec} \theta)(1 + \tan \theta + \sec \theta)$$

$$= \left(1 + \frac{\cos \theta}{\sin \theta} - \frac{1}{\sin \theta}\right) \left(1 + \frac{\sin \theta}{\cos \theta} + \frac{1}{\cos \theta}\right)$$

( $\frac{1}{2}$  mark)

$$= \left(\frac{\sin \theta + \cos \theta - 1}{\sin \theta}\right) \left(\frac{\cos \theta + \sin \theta + 1}{\cos \theta}\right)$$

( $\frac{1}{2}$  mark)

$$= \frac{(\sin \theta + \cos^2 \theta) - (1)^2}{\sin \theta \cos \theta}$$

( $\frac{1}{2}$  mark)

$$= \frac{\sin^2 \theta + \cos^2 \theta + 2 \sin \theta \cos \theta - 1}{\sin \theta \cos \theta}$$

( $\frac{1}{2}$  mark)

$$= \frac{1 + 2 \sin \theta \cos \theta - 1}{\sin \theta \cos \theta}$$

( $\frac{1}{2}$  mark)



$$= \frac{2 \sin \theta \cos \theta}{\sin \theta \cos \theta} = 2 \quad \left( \frac{1}{2} \text{ mark} \right)$$

Ans19 Let  $\frac{1}{x+y} = a, \frac{1}{y-x} = b$

$$10a + 4b = -2 \quad \rightarrow \quad (1) \quad \left( \frac{1}{2} \text{ mark} \right)$$

$$15a - 7b = 10 \quad \rightarrow \quad (2)$$

(1)  $\times$  3 and (2)  $\times$  2 gives

$$\cancel{30}a + 12b = -6$$

$$\cancel{30}a - 14b = 20$$

$$\hline 26b = -26$$

$$\Rightarrow b = -1$$

(1 mark)

Substituting  $b = -1$  in (1):

$$10a - 4 = -2$$

$$\Rightarrow 10a = 2$$

$$\Rightarrow a = \frac{1}{5}$$

$\left( \frac{1}{2} \text{ mark} \right)$

$$\therefore x + y = 5$$

$$\hline -x + y = -1$$

$$2y = 4 \Rightarrow y = 2$$

$$\therefore x = 3$$

(1 mark)

OR

For real and distinct roots:  $D > 0$

$\left( \frac{1}{2} \text{ mark} \right)$

Discriminant  $D = b^2 - 4ac$

$$\left[ -2(1+2m) \right]^2 - 4(2m)(3+2m) > 0$$

$\left( \frac{1}{2} \text{ mark} \right)$

$$4(1+2m)^2 - 4(2m)(3+2m) > 0$$

$$1 + \cancel{4m^2} + 4m - 6m - \cancel{4m^2} > 0$$

$\left( \frac{1}{2} \text{ mark} \right)$



$$1 - 2m > 0$$

$\left(\frac{1}{2} \text{ mark}\right)$

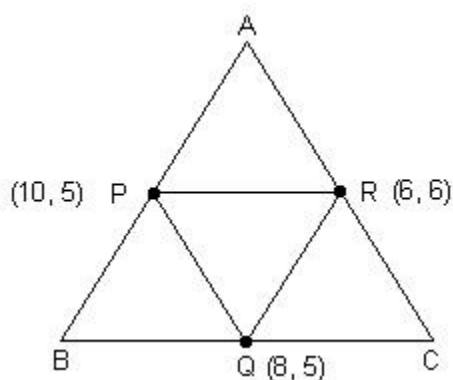
$$\Rightarrow 1 > 2m$$

$$\Rightarrow \frac{1}{2} > m$$

$$\Rightarrow m < \frac{1}{2}$$

(1 mark)

Ans20



(1 mark)

We know that area of triangle formed by joining the midpoint of sides of a triangle is  $\frac{1}{4}$ th the area of the triangle.

$$\text{ar}(\Delta PQR) = \frac{1}{4} (\text{ar } \Delta ABC)$$

$\left(\frac{1}{2} \text{ mark}\right)$

$$\text{ar}(\Delta PQR) = \frac{1}{2} [10(6-5) + 6(5-5) + 8(5-6)]$$

(1 mark)

$$= \frac{1}{2} [10 - 8]$$

$$= 1 \text{ sq unit}$$

$$\text{So ar } (\Delta ABC) = 4 \text{ sq unit}$$

$\left(\frac{1}{2} \text{ mark}\right)$



Ans21  $3x^2 - 11x + 14$

$$\alpha + \beta = \frac{11}{3}, \quad \alpha\beta = \frac{14}{3} \quad (1 \text{ mark})$$

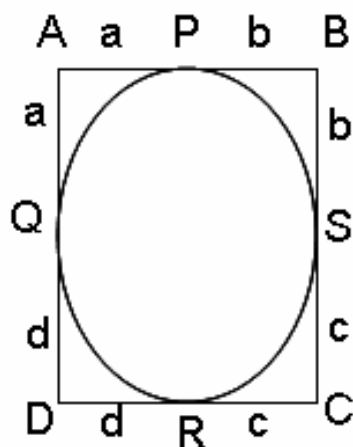
$$\alpha + \beta^2 = (\alpha + \beta)^2 - 2\alpha\beta \quad (1 \text{ mark})$$

$$= \left(\frac{11}{3}\right)^2 - 2\left(\frac{14}{3}\right) \quad \left(\frac{1}{2} \text{ mark}\right)$$

$$= \frac{121}{9} - \frac{28}{3} \quad \left(\frac{1}{2} \text{ mark}\right)$$

$$= \frac{37}{9}$$

Ans22 We know that tangents drawn from an external point are equal.



$\therefore$  Let  $AP = AQ = a$   
 $BP = BS = b$   
 $CS = CR = c$   
 $DQ = DR = d$  ( $\frac{1}{2}$  mark)

Since ABCD is a parallelogram, opposite sides are equal.

$$\cancel{a} + b = \cancel{c} + d \quad \left(\frac{1}{2} \text{ mark}\right)$$

$$\cancel{a} + d = \cancel{c} + b$$

on subtracting , we get



$$b - d = d - b$$

$$\Rightarrow 2b = 2d$$

$$\Rightarrow b = d$$

$$\therefore AB = a + b$$

$$= a + d$$

$$= AD$$

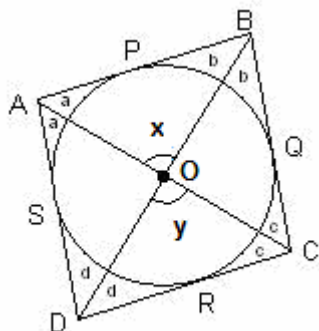
$\left(\frac{1}{2} \text{ mark}\right)$

Since adjacent sides are equal ABCD is a rhombus.

$\left(\frac{1}{2} \text{ mark}\right)$

OR

We know that the two tangents drawn from an external point are equally inclined to the line joining the point and centre  $\left(\frac{1}{2} \text{ mark}\right)$



$\left(\frac{1}{2} \text{ mark}\right)$

$$\therefore \text{ Let } \angle OAP = \angle OAS = a \quad \angle OCQ = \angle OCR = c$$

$$\angle OBP = \angle OBQ = b \quad \angle ODR = \angle ODS = d$$

$\left(\frac{1}{2} \text{ mark}\right)$

$$\text{In } \triangle AOB : a + b + x = 180^\circ$$

$$\text{In } \triangle COD : c + d + y = 180^\circ$$

$\left(\frac{1}{2} \text{ mark}\right)$

$$\text{On adding } a + b + c + d + x + y = 360$$

$\left(\frac{1}{2} \text{ mark}\right)$

$$\Rightarrow 180 + x + y = 360$$

(Using angle sum property of quadrilateral  $2a + 2b + 2c + 2d = 360$ )

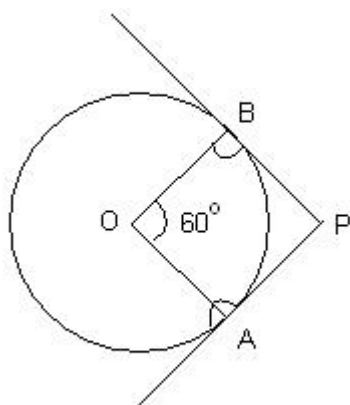


So  $x + y = 180^\circ$

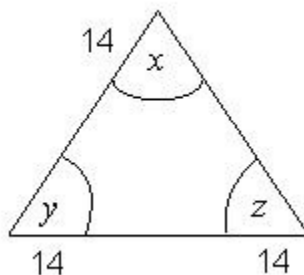
$\left(\frac{1}{2} \text{ mark}\right)$

Hence proved.

- Ans23 Construction of circle and 2 radii OA,OB at an angle of  $60^\circ$  (1 mark)  
 Construction of tangents through the points on the circle (2 marks)



- Ans24 Let the angles of triangle be  $x, y, z$ .



Area grazed by the three horses

$$= \frac{x}{360} \pi r^2 + \frac{y}{360} \pi r^2 + \frac{z}{360} \pi r^2 \quad (1 \text{ mark})$$

$$= \frac{\pi r^2}{360} (x + y + z) \quad \left(\frac{1}{2} \text{ mark}\right)$$



$$= \frac{\pi r^2}{360} \times 180 \quad \left(\frac{1}{2} \text{ mark}\right)$$

$$= \frac{22}{7} \times 14 \times 14 \times \frac{1}{2} \quad \left(\frac{1}{2} \text{ mark}\right)$$

$$= 308 \text{ m}^2 \quad \left(\frac{1}{2} \text{ mark}\right)$$

Ans25  $a_{46} = 25$

$$\Rightarrow a + 45d = 25 \quad \left(\frac{1}{2} \text{ mark}\right)$$

$$S_{91} = \frac{91}{2} [2a + 90d] \quad (1 \text{ mark})$$

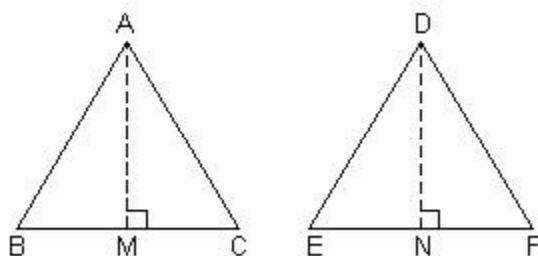
$$= 91(a + 45d) \quad \left(\frac{1}{2} \text{ mark}\right)$$

$$= 91 \times 25 \quad \left(\frac{1}{2} \text{ mark}\right)$$

$$= 2275 \quad \left(\frac{1}{2} \text{ mark}\right)$$

**Section D**

Ans26 Given:  $\Delta ABC \sim \Delta DEF$



To Prove:  $\frac{\text{ar}(\Delta ABC)}{\text{ar}(\Delta DEF)} = \frac{AB^2}{DE^2} = \frac{BC^2}{EF^2} = \frac{AC^2}{DF^2}$

Construction: Draw  $AM \perp BC$  and  $DN \perp EF$

Proof: In  $\Delta ABC$  and  $\Delta DEF$  (1mark)

$$\frac{\text{ar}(\Delta ABC)}{\text{ar}(\Delta DEF)} = \frac{\frac{1}{2} \times BC \times AM}{\frac{1}{2} \times EF \times DN} = \frac{BC}{EF} \cdot \frac{AM}{DN} \quad \dots(i)$$



$$\left[ \text{Area of } \Delta = \frac{1}{2} \times \text{base} \times \text{corresponding altitude} \right]$$

$\therefore \Delta ABC \square \Delta DEF \quad \dots(\text{Given})$   
 $\therefore \frac{AB}{DE} = \frac{BC}{EF} \quad \dots(\text{Sides are proportional})\dots(\text{ii})$   
 $\angle B = \angle E \quad \dots(\because \Delta ABC \square \Delta DEF)$   
 $\angle M = \angle N \quad \dots(\text{each } 90^\circ)$   
 $\therefore \Delta ABM \square \Delta DEN \quad \dots(\text{AA Similarity})$   
 $\therefore \frac{AB}{DE} = \frac{AM}{DN} \quad \dots(\text{iii})[\text{Sides are proportional}]$

From (ii) and (iii), we have

$$\frac{BC}{DE} = \frac{AM}{DN} \quad (1 \text{ mark})$$

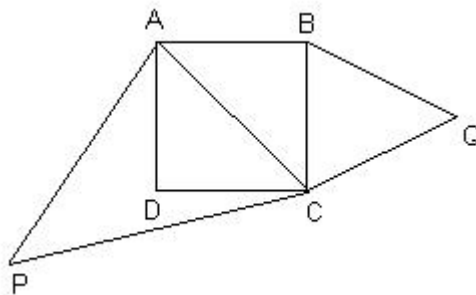
From (i) and (iv), we have

$$\frac{\text{ar}(\Delta ABC)}{\text{ar}(\Delta DEF)} = \frac{BC}{EF} \cdot \frac{BC}{EF} = \frac{BC^2}{EF^2}$$

Similarly, we can prove that

$$\frac{\text{ar}(\Delta ABC)}{\text{ar}(\Delta DEF)} = \frac{AB^2}{DE^2} = \frac{AC^2}{DF^2}$$

$\therefore \frac{\text{ar}(\Delta ABC)}{\text{ar}(\Delta DEF)} = \frac{AB^2}{DE^2} = \frac{BC^2}{EF^2} = \frac{AC^2}{DF^2} \quad (2 \text{ marks})$



$\Delta ABC$  and  $\Delta ACP$  are equilateral triangles and therefore similar.

(1 mark)





$$AC^2 = AB^2 + BC^2 = 2BC^2 \quad (\text{By Pythagoras theorem}) \quad \left(\frac{1}{2} \text{ mark}\right)$$

Using the above theorem

$$\frac{\text{area } \square ACP}{\text{area } \square BCQ} = \frac{AC^2}{BC^2} = \frac{2BC^2}{BC^2} = 2 \quad \left(\frac{1}{2} \text{ mark}\right)$$

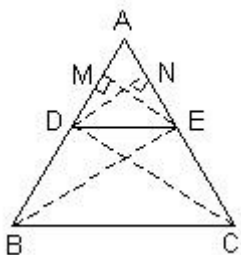
OR

Statement: If a line is drawn parallel to one side of a triangle to intersect the other two sides in distinct points, the other two sides are divided in the same ratio. (1 Mark)

Given: In  $\triangle ABC$ ,  $DE \parallel BC$

To prove:  $\frac{AD}{DB} = \frac{AE}{EC}$

Construction: Draw  $EM \perp AD$  and  $DN \perp AE$ . Join B to E and C to D



(1 mark)

Proof: In  $\triangle ADE$  and  $\triangle BDE$

$$\frac{\text{ar}(\triangle ADE)}{\text{ar}(\triangle BDE)} = \frac{\frac{1}{2} \times AD \times EM}{\frac{1}{2} \times DB \times EM} = \frac{AD}{DB} \quad \dots(i)$$

$$[\text{Area of } \triangle = \frac{1}{2} \times \text{base} \times \text{corresponding altitude}]$$



In  $\triangle ADE$  and  $\triangle CDE$

$$\frac{\text{ar}(\triangle ADE)}{\text{ar}(\triangle CDE)} = \frac{\frac{1}{2} \times AE \times DN}{\frac{1}{2} \times EC \times DN} = \frac{AE}{EC} \quad \dots(ii)$$

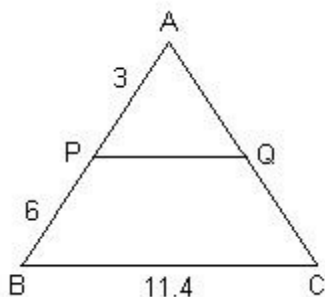
$\therefore DE \parallel BC \quad \dots(\text{Given})$

$\therefore \text{ar}(\triangle BDE) = \text{ar}(\triangle CDE) \quad \dots(iii)$

( $\because$   $\Delta$ s on the same base and between the same parallel sides are equal in area)

From (i), (ii) and (iii)

$$\frac{AD}{DB} = \frac{AE}{EC} \quad (2 \text{ marks})$$



Since  $PQ \parallel BC$   
 $\triangle APQ \sim \triangle ABC$  (By AA condition) (1 mark)



$$\begin{aligned} \therefore \frac{AP}{AB} &= \frac{PQ}{BC} \\ \Rightarrow \frac{3}{9} &= \frac{PQ}{11.4} && (1 \text{ mark}) \\ \Rightarrow PQ &= \frac{34.2}{9} = 3.8 \text{ cm} \end{aligned}$$

Ans27 Let length of rectangle = x m

Breadth = y m

$$\text{Area} = xy \text{ m}^2. \quad \left(\frac{1}{2} \text{ mark}\right)$$

$$(x+7)(y-3) = xy \quad (1 \text{ mark})$$

$$\Rightarrow -3x + 7y - 21 = 0 \rightarrow (1) \quad \left(\frac{1}{2} \text{ mark}\right)$$

$$(x-7)(y+5) = xy \quad (1 \text{ mark})$$

$$5x - 7y - 35 = 0 \rightarrow (2) \quad \left(\frac{1}{2} \text{ mark}\right)$$

(1) + (2) gives:

$$2x - 56 = 0$$

$$\Rightarrow x = 28 \text{ m} \quad (1 \text{ mark})$$

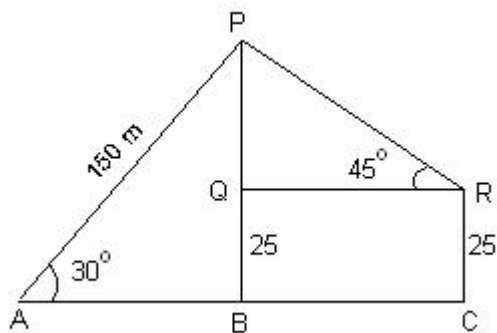
On substituting x = 28 m in equation (2), we get y = 15 m

The length is 28 m and the breadth is 15m.  $\left(\frac{1}{2} \text{ mark}\right)$

Therefore, area is 420m<sup>2</sup>  $(1 \text{ mark})$



Ans28 A and R are the positions of the two boys. P is the point where the two kites meet. ( $\frac{1}{2}$  mark)



(1 mark)

In  $\Delta ABP$

$$\sin 30^\circ = \frac{PB}{AP}$$

$$\frac{1}{2} = \frac{PB}{150}$$

$$\Rightarrow PB = 75m$$

and  $QB = 25m$

$$\Rightarrow PQ = 50m$$

( $1\frac{1}{2}$  mark)

(1 mark)

In  $\Delta PQR$

$$\sin 45^\circ = \frac{PQ}{PR}$$

$$\frac{1}{\sqrt{2}} = \frac{50}{PR}$$

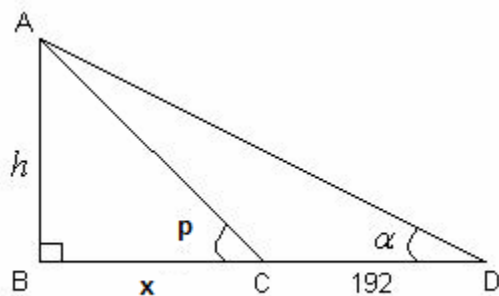
$$\Rightarrow 50\sqrt{2} = PR$$

( $1\frac{1}{2}$  mark)

$\therefore$  The boy should have a string of length 70.7m

( $\frac{1}{2}$  mark)

OR



(1 mark)

D is the initial point of observation and C is the next point of observation.

AB is the tower of height  $h$ . Let  $BC = x$

$$\tan \alpha = \frac{AB}{BD} \qquad \left(\frac{1}{2} \text{ mark}\right)$$

$$\frac{5}{12} = \frac{h}{x+192}$$

$$\Rightarrow 12h - 5x - 960 = 0 \rightarrow (1) \qquad (1 \text{ mark})$$

$$\tan p = \frac{AB}{BC} \qquad \left(\frac{1}{2} \text{ mark}\right)$$

$$\frac{3}{4} = \frac{h}{x}$$

$$\Rightarrow 3x = 4h \rightarrow (2) \qquad (1 \text{ mark})$$

From (2):  $12h = 9x$  and substituting in (1):

$$9x - 5x = 960$$

$$4x = 960 \qquad (1 \text{ mark})$$

$$\Rightarrow x = 240$$

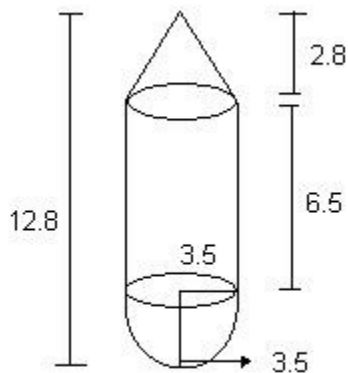
$$\therefore h = \frac{3 \times 240}{4} \text{ from (2)} \qquad \left(\frac{1}{2} \text{ mark}\right)$$

$$= 180$$

$$\therefore \text{The height of the tower is } 180 \text{ m.} \qquad \left(\frac{1}{2} \text{ mark}\right)$$



Ans29



$$\begin{aligned} \text{Height of cone} &= 12.8 - (6.5 + 3.5) \\ &= 2.8 \text{ c} \end{aligned} \quad (1 \text{ mark})$$

$$\begin{aligned} \text{Slant height } l &= \sqrt{(3.5)^2 + (2.8)^2} \\ &= \sqrt{12.25 + 7.84} \\ &= \sqrt{20.09} \\ &= 4.48 \end{aligned} \quad \left(1\frac{1}{2} \text{ mark}\right)$$

$$\begin{aligned} TSA &= 2\pi r^2 + 2\pi rh + \pi rl \\ &= \pi r(2r + 2h + l) \\ &= \frac{22}{7} \times \frac{7}{2} (7 + 13 + 4.48) \end{aligned} \quad (1 \text{ mark})$$

$$\begin{aligned} &= 11 \times 24.48 \\ &= 269.28 \end{aligned} \quad \left(1\frac{1}{2} \text{ mark}\right)$$

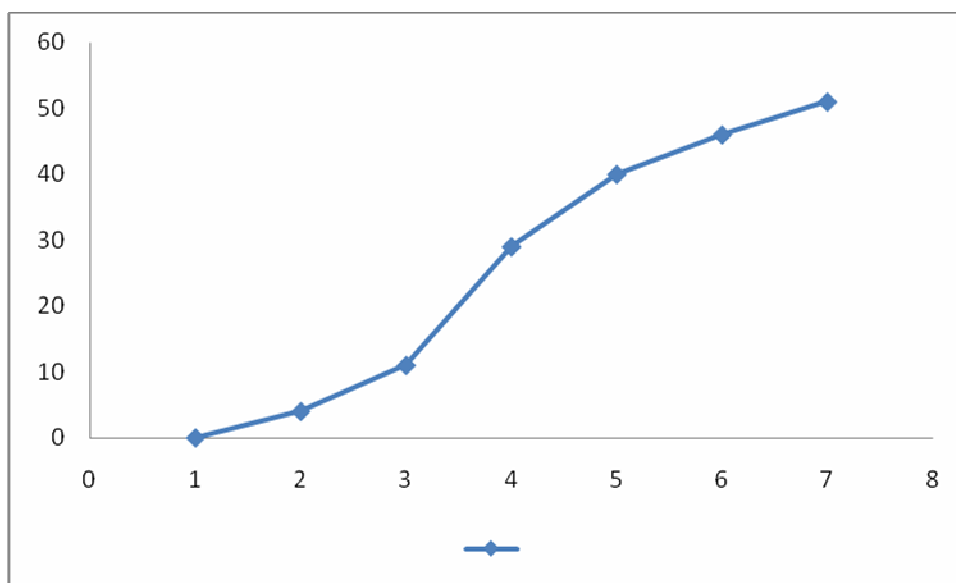
$$\therefore \text{The surface area of the solid is } 269.28 \text{ cm}^2 \quad \left(\frac{1}{2} \text{ mark}\right)$$



Ans30

<i>CI</i>	<i>f</i>	<i>C.f</i>
Less than 140	4	4
140 - 145	7	11
<u>145 - 150</u>	18	29
150 - 155	11	40
155 - 160	6	46
160 - 165	5	51
	<u>51</u>	

(2 marks)



(2 marks)

$$n = 51 \Rightarrow \frac{n}{2} = 25.5$$

Median class = 145 - 150

$$\text{Median} = l + \left( \frac{\frac{n}{2} - cf}{f} \right) h$$



$$= 145 + \left( \frac{25.5 - 11}{18} \right) 5$$

$$= 145 + \frac{14.5 \times 5}{18}$$

$$= 145 + \frac{72.5}{18}$$

$$= 149.02$$

(2 marks)